~ Section 4.1 Notes ~ Graphing Relationships

TLW match simple graphs with situations

TLW graph a relationship

TLW describe relationships as increasing, decreasing or constant



State whether each word or phrase represents an amount that is increasing, decreasing, or constant.

1. Stays the same

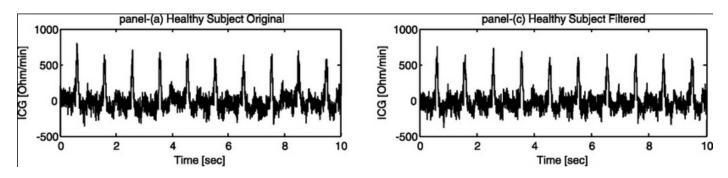
2. Rises

3. Drops

4. Slows down

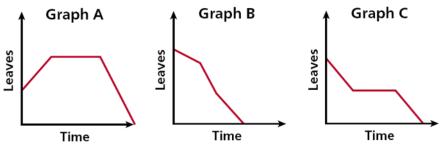
Graphs Can be used to illustrate many different situations.

For example, trends shown on a Cardiograph Can help a doctor see how a patient's heart is functioning. To relate a graph to a given situation, use key words in the description.



Example 1 - Relating Graphs to Situations

Each day several leaves fall from a tree. One day a gust of wind blows off many leaves. Eventually, there are no more leaves on the tree. Choose the graph that best represents the situation.

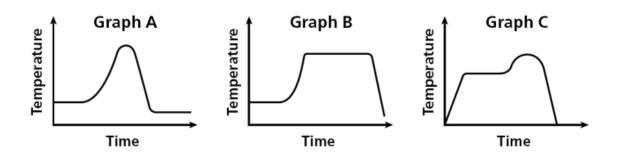


Fill in the table based on the above example.

Key Words	Segment Description	Graphs
Each day several leaves fall	Never horizontal	
Wind blows off many leaves	Slanting downward rapidly	
Eventually no more leaves	Slanting downward until reaches zero	

<u>Example 2</u>

The air temperature increased steadily for several hours and then remained constant. At the end of the day, the temperature increased slightly before dropping sharply. Choose the graph that best represents this situation.



Fill in the table based on the above example.

Key Words	Segment Description	Graphs
Increased steadily	Slanting upward	
Remained constant	Horizontal	
Increased slightly before dropping sharply	Slanting upward and then steeply downward	

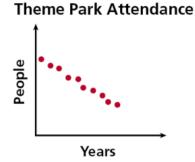
As seen in Example 1, some graphs are connected lines or curves called _____

Some graphs are only distinct points. They are called _____

•

•

The graph on theme park attendance is an example of a discrete graph. It consists of distinct points because each year is distinct and people are counted in whole numbers only. The values between whole numbers are not included, since they have no meaning for the situation.



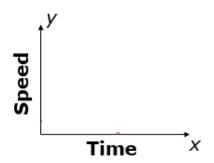
Sketching Graphs for Situations

<u>Example 1</u>

Sketch a graph for the situation. Tell whether the graph is continuous or discrete. A truck driver enters a street, drives at a constant speed, stops at a light, and then continues.

As time passes during the trip (moving left to right along the x-axis) the truck's speed (y-axis) does the following:

- initially increases
- remains Constant
- decreases to a stop
- increases
- remains constant



The graph is _____.

<u>Example 2</u>

Tell whether the graph is continuous or discrete. A small bookstore sold between 5 and 8 books each day for 7 days.

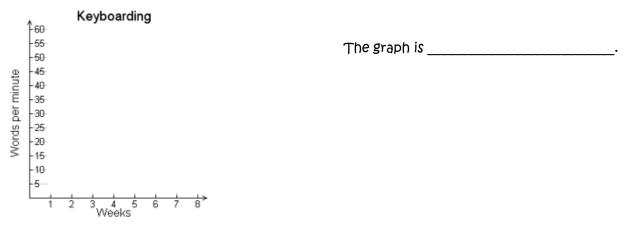


The graph is _____.

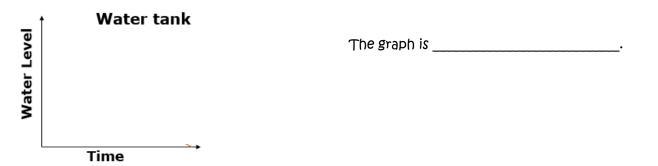
Guided Practice

Sketch a graph for the situation. Tell whether the graph is continuous or discrete.

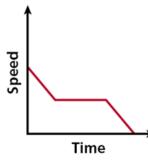
1. Jamie is taking an 8-week keyboarding Class. At the end of each week, she takes a test to find the number of words she Can type per minute. She improves each week.



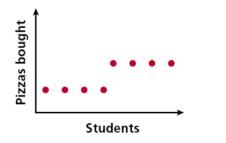
2. Henry begins to drain a water tank by opening a valve. Then he opens another valve. Then he closes the first valve. He leaves the second valve open until the tank is empty.



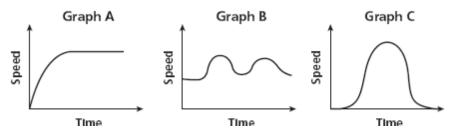
3. Write a possible situation for the given graph.



4. Write a possible situation for the given graph.



Choose the graph that best represents each situation. Write A, B, or C on the line provided.



1.) A person alternates between running and walking.

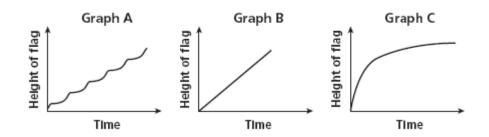
2.) A person gradually speeds up to a constant running pace.

3.) A person walks, gradually speeds up to a run, and then slows back down to a walk.

Choose the graph that best represents each situation. Write A, B, or C on the line provided.

- 4.) A flag is raised up a flagpole quickly at the beginning and then more slowly near the top.
- 5.) A flag is raised up a flagpole in a jerky motion, using a hand-over-hand method.

6.) A flag is raised up a flagpole at a constant rate of speed.

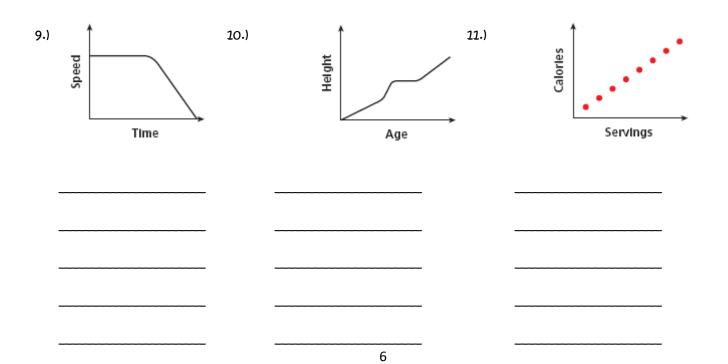


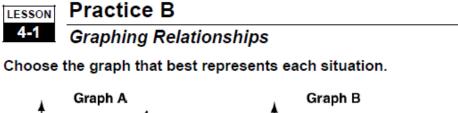
Graph the following situations.

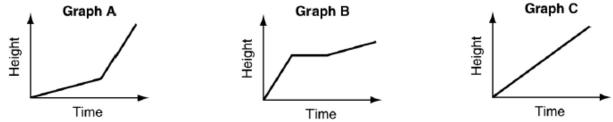
7.) Maddie is buying extra pages for her photo album. Each page holds exactly 8 photos. Sketch a graph to show the maximum number of photos she can add to her album if she buys 1, 2, 3, or 4 extra pages. Tell whether the graph is continuous or discrete.

8.) For six months, a puppy gained weight at a steady rate. Sketcha graph to illustrate the weight of the puppy during that time period.Tell whether the graph is continuous or discrete.

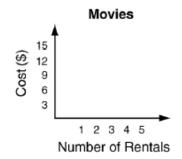
Write a possible situation for each graph.



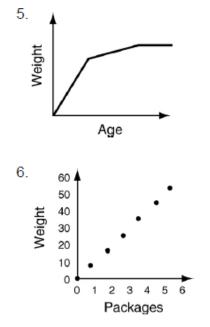


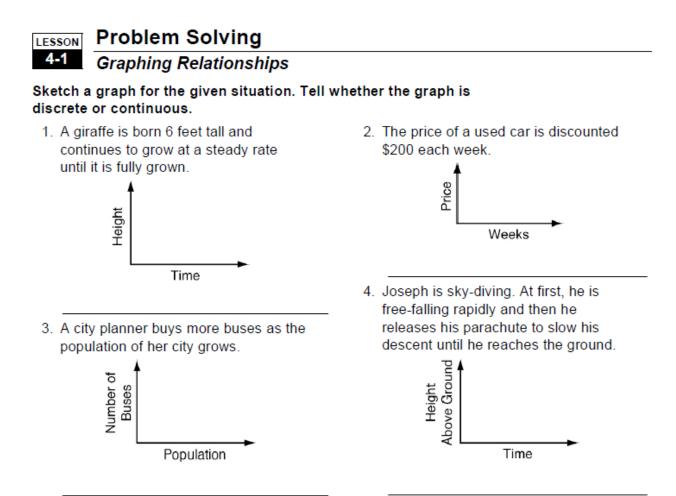


- 1. A tomato plant grows taller at a steady pace.
- A tomato plant grows quickly at first, remains a constant height during a dry spell, then grows at a steady pace.
- A tomato plant grows at a slow pace, then grows rapidly with more sun and water.
- Lora has \$15 to spend on movie rentals for the week. Each rental costs \$3.
 Sketch a graph to show how much money she might spend on movies in a week. Tell whether the graph is continuous or discrete.



Write a possible situation for each graph.





Choose the graph that best represents the situation.

 Rebekah turns on the oven and sets it to 300 °F. She bakes a tray of cookies and then turns the oven off.

A Graph 1	C Graph 3
-----------	-----------

B Graph 2 D Graph 4

Leon puts ice cubes in his soup to cool it down before eating it.

F Graph 1 H		Graph	3
-------------	--	-------	---

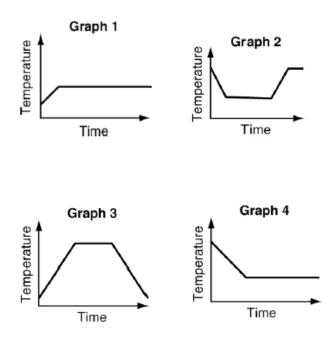
G Graph 2	J Graph 4
-----------	-----------

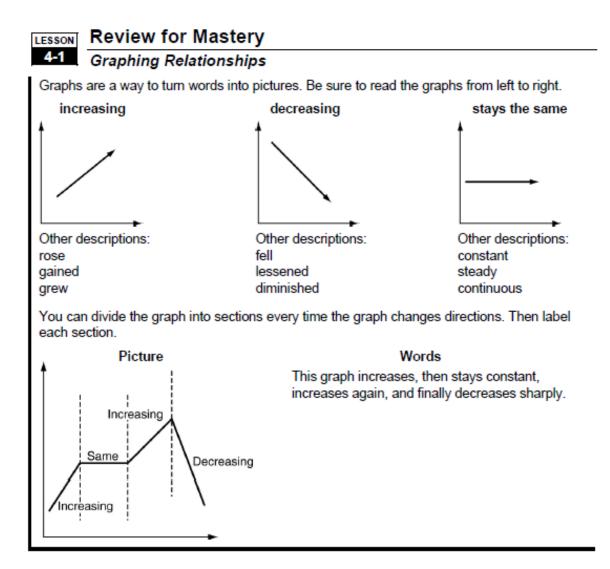
 Barlee has the flu and her temperature rises slowly until it reaches 101 °F.

A Graph 1	C Graph 3
B Graph 2	D Graph 4

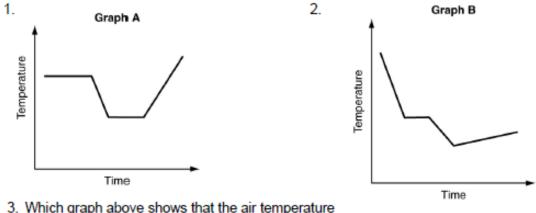
 On a hot day, Karin walks into and out of an air-conditioned building.

F Graph 1	H Graph 3
G Graph 2	J Graph 4

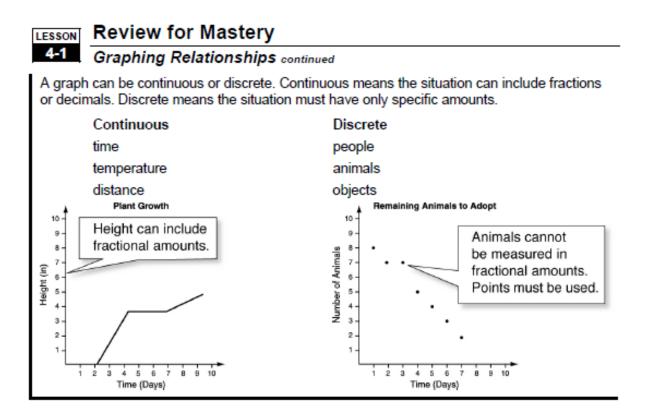




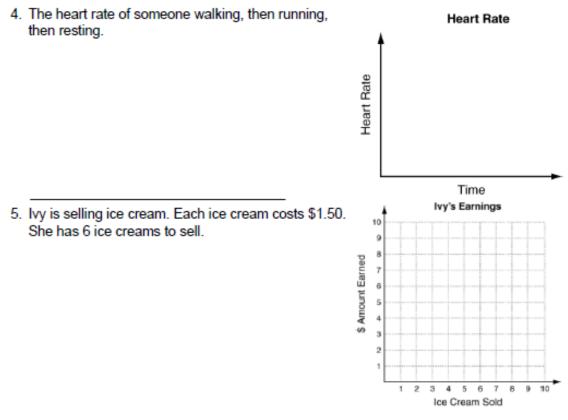
Divide each graph into sections where the graph changes directions. Then label the sections as *increasing, decreasing,* or *same*.



3. Which graph above shows that the air temperature fell steadily, leveled off, fell again, and then increased slightly?



Sketch a graph of each situation. Tell whether the graph is continuous or discrete.



~ Section 4.2 Notes ~ Relations \Rightarrow Functions

TLW identify functions

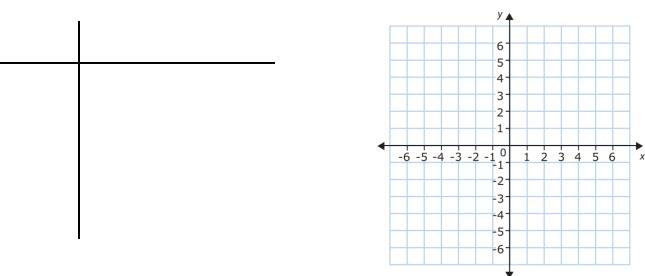
TLW find the domain and range of relations and functions

TLW define relation, function, domain and range



Quick Draw Review

Generate ordered pairs for the function y = x+3 for x = -2, -1, 0, 1, and 2



In Lesson 4-1 you saw relationships represented by graphs. Relationships Can also be represented by a set of ordered pairs Called a ______.

For example:

In the scoring systems of some track meets, for first place you get 5 points, for second place you get 3 points, for third place you get 2 points, and for fourth place you get 1 point.

This scoring system is a relation, so it Can be shown by ordered pairs:

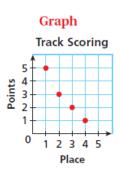
 $\left\{ (\ , \), (\ , \), (\ , \), (\ , \), (\ , \) \right\}$

Example 1 - All Written Out Just for You!

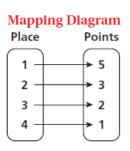
Express the relation for the track meet scoring system, $\{(1,5), (2,3), (3,2), (4,1)\}$

Table		
Track Scoring		
Place Points		
1	5	
2	3	
3	2	
4	1	

Write all x-values under "Place" and all y-values under "Points."



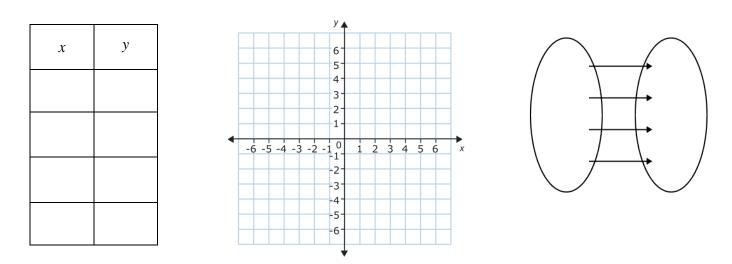
Use the x- and y-values to plot the ordered pairs.



Write all x-values under "Place" and all y-values under "Points." Draw an arrow from each x-value to its corresponding y-value.

Example 2 - Now You Try!

Express the relation $\{(2,3), (4,6), (1,4), (3,2)\}$ as a table, as a graph, and as a mapping diagram.



The domain of the track meet scoring system is $\{$

The range is $\{$

}

For each of the examples state the domain and range of the relations.

	2. 6 5 2 -4 -1	3.	× 1 4	У 1 4	
$0 \frac{1}{2} \frac{1}{4}$			8	1	
Domain:	Domain:	Dom	nain:		
Range:	Range:	Rang	ge:		
is a specialis a special	type of relation that pairs each do	main value with	n exaCt	ly one ra	ange Value

Function or Relation - You Tell Me!

Example 1

Give the domain and range of the relation. Tell whether the relation is a function. Explain.

{(3,-2),(5,-	1), (4, 0),	(3,1)}
$((\cdot ,), (\cdot ,))$	$\mathcal{F}(\mathcal{F})$	(-,))

Yes, It's a Function / No, It's Not a Function

Domain: _____

Range:

Example 2

Give the domain and range of the relation. Tell whether the relation is a function. Explain.

-4	
-8-	-2
-0	-1
4	
5	\sim

Yes, It's a Function / No, It's Not a Function

Domain: _____

Range:

Guided Practice

Give the domain and range of each relation. Tell whether the relation is a function and explain.

1.	$\{(-1,1),(-3,3),(5,-5),(-7,7)\}$		No, It's Not a Function
2.	$\{(-5,7),(0,0),(2,-8),(5,-20)\}$		No, It's Not a Function
з.	x 3 5 2 8 6 y 9 25 4 81 36		/ No, It's Not a Function
4.	x -2 -1 0 1 2 y 1 1 1 1 1	Domain: _	/ No, It's Not a FunCtion
5.	5 4 3 2 1 0 1 2 3 4 5	Domain:	/ No, It's Not a FunCtion
6.	3 ¹ / ₂ 2 0 2 ^X -3 -	Domain: _	/ No, It's Not a FunCtion

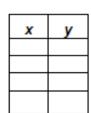
LESSON Practice B

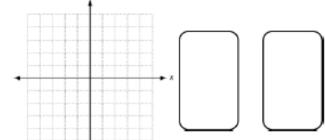
4-2

Relations and Functions

Express each relation as a table, as a graph, and as a mapping diagram. χ

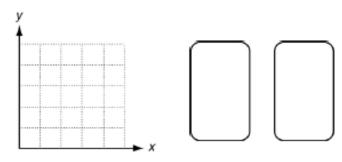
1. {(-5, 3), (-2, 1), (1, -1), (4, -3)}



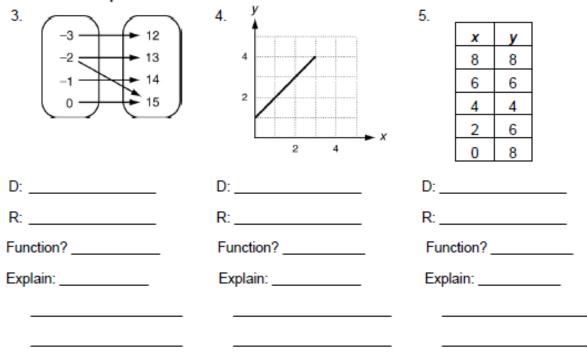


2. {(4, 0) (4, 1), (4, 2), (4, 3), (4, 4), (4, 5)}

x	y



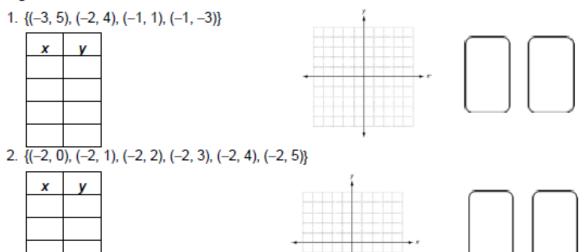
Give the domain and range of each relation. Tell whether the relation is a function. Explain.



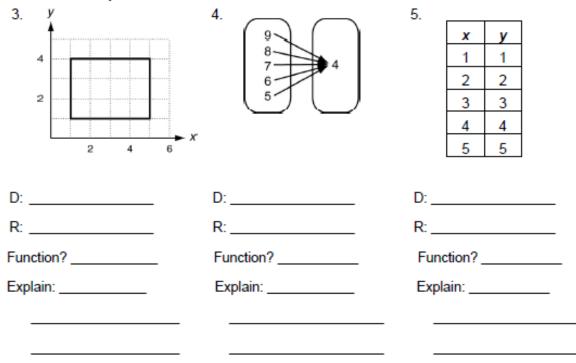
LESSON Practice C

4-2 Relations and Functions

Express each relation as a table, as a graph, and as a mapping diagram.



Give the domain and range of each relation. Tell whether the relation is a function. Explain.



LESSON Problem Solving

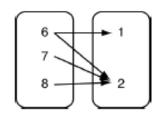
4-2

Relations and Functions

Give the domain and range of each relation and tell whether it is a function.

2.

 The mapping diagram shows the ages x and grade level y of four children.



Age x	Shoe Size y
6	8
9	10
12	10
15	10.5
18	11

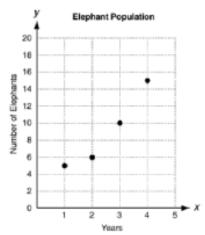
- The list represents the number of cars sold and the bonus received by the salespeople of a car dealership. {(1, 50), (2, 50), (3, 100), (4, 150)}
- A 2-inch-tall plant grows at a rate of 2.5 inches every week for 5 weeks. Let x represent the number of weeks and y represent the height of the plant.

Use the graph below to answer questions 5–6. A conservation group has been working to increase the population of a herd of Asian elephants. The graph shows the results of their efforts. Select the correct answer.

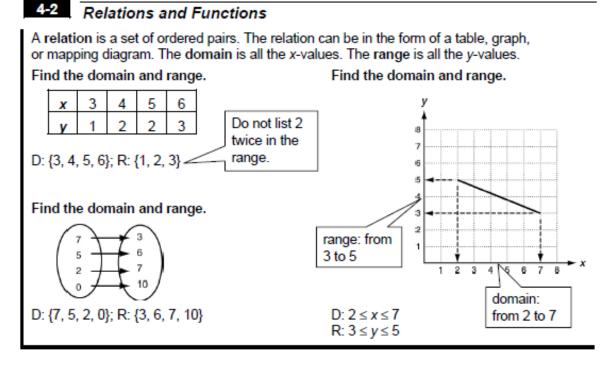
- 5. Which relation represents the information in the graph?
 - A {(1, 4.5), (2, 6), (3, 10), (4, 14.5)}
 - B {(1, 5), (2, 6), (3, 10), (4, 15)}
 - C {(4.5, 1), (6, 2), (10, 3), (14.5, 4)}
 - D {(5, 1), (6, 2), (10, 3), (15, 4)}

6. What is the range of the relation shown in the graph?

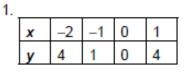
- F {0, 1, 2, 3, 4, 5}
- G {1, 2, 3, 4}
- H {4.5, 6, 10, 14.5}
- J {5, 6, 10, 15}

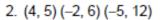


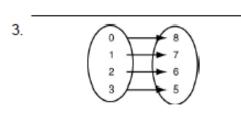
LESSON Review for Mastery

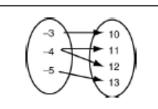


Find the domain and range of each relation.

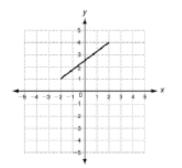


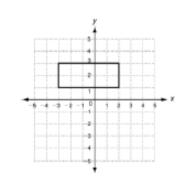






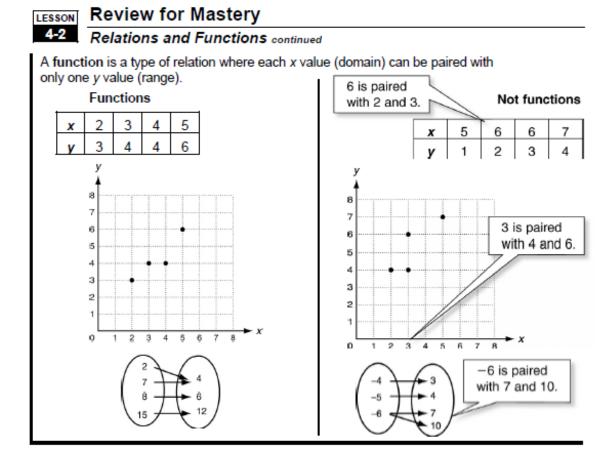
5.



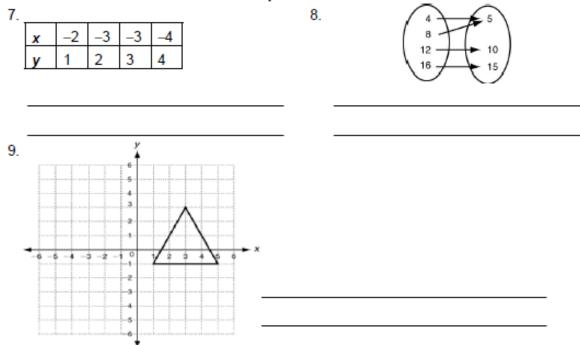


4.

6.



Tell whether the relation is a function. Explain.



~ Section 4.3 Notes ~ Writing Functions

TLW identify independent and dependent variables

TLW write an equation in function notation and evaluate a function given input values

TLW define new vocabulary words such as: independent variable, dependent variable, function rule and function notation



Quick Draw Review

Evaluate each expression for a = 2, b = -3 and c = 8.

1. a+3c **2.** ab-c **3.** $\frac{1}{2}c+b$ **4.** b^a+c

Using a Table to Write a Function

Example 1 - All Done For You!

Determine a relationship between the x-values and y-values. Write an equation.

x	5	10	15	20
y	1	2	3	4

Step 1 List possible relationships between the first *x* and *y*-values.

$$5 - 4 = 1 \text{ and } 5\left(\frac{1}{5}\right) = 1$$

Step 2 Determine which relationship works for the other x- and y- values.

 $10 - 4 \neq 2 \quad \text{and} \quad 10\left(\frac{1}{5}\right) = 2$ $15 - 4 \neq 3 \quad \text{and} \quad 15\left(\frac{1}{5}\right) = 3$ $20 - 4 \neq 4 \quad \text{and} \quad 20\left(\frac{1}{5}\right) = 4$ The value of y is one-fifth, $\left(\frac{1}{5}\right)$, of x.

Step 3 Write an equation.

 $y = \frac{1}{5}x$ or $y = \frac{x}{5}$ The value of y is one-fifth of x.

Example 2 – Let's Do This One Together

Determine a relationship between the x-values and y-values. Write an equation.

 $\{(1,3),(2,6),(3,9),(4,12)\}$

x		
У		

Example 3 – You Try!

Determine a relationship between the x-values and y-values. Write an equation.

 $\{(1,-2),(2,-1),(3,0),(4,1)\}$

x		
У		

Independent & Dependent Variables

The input of a function is the _____.

The output of a function is the _____

The value of the dependent variable *depends* on, or is a function of, the value of the independent variable.

Example 1 – All Worked Out for You

Identify the independent and dependent variable in the situation.

A painter must measure a room before deciding how much paint to buy.

The amount of paint *depends on* the measurement of a room.

Dependent: amount of paint Independent: measurement of the room Example 2 – Let's Do This One Together

Identify the independent and dependent variable in the situation.

In the winter, more electricity is used when the temperature goes down and less is used when the temperature rises.

Dependent:

Independent:

<u>Example 3</u> – You Try! Identify the independent and dependent variable in the situation.

The cost of shipping a package is based on its weight.

Dependent:

Independent:

Try a couple more...

Identify the independent and dependent variable in the situation.

(a) A veterinarian must weigh an animal before determining the amount of medication.

Dependent: Independent:

(b) A company charges \$10 per hour to rent a jackhammer.

Dependent: Independent:

(C) The height of a candle decreases 1 cm for every hour it burns.

Dependent:

Independent:

An algebraic expression that defines a function is a *function rule*.

If x is the independent variable and y is the dependent variable, then <u>function notation</u> for y is f(x) read "f of x," where f names the function. When an equation in two variables describes a function, you can use function notation to write it.

The dependent variable is a function of the independent variable. y is a function of x. y = f (x)

Writing Functions

Example 1 – All Worked Out for You!

Identify the independent and dependent variables. Write a rule in function notation for the situation.

A math tutor charges \$35 per hour.

The amount a math tutor charges depends on number of hours.

Dependent: charges Independent: hours

Let *h* represent the number of hours of tutoring.

The function for the amount a math tutor charges is f(h) = 35h.

Example 2 – Let's Try This One Together

Identify the independent and dependent variables. Write a rule in function notation for the situation.

A fitness Center Charges a \$100 initiation fee plus \$40 per month.

The	depends on th	?	, plus \$100.
1110			; F100 #200;

Dependent:

Independent:

Let m represent the number of months

The function for the amount the fitness center charges is f(m)

<u>Example 3</u> – You Try! Identify the independent and dependent variables. Write a rule in function notation for the situation.

Steven buys lettuce that costs \$1.69/lb.

<u>Example 4</u> – You Try Again! Identify the independent and dependent variables. Write a rule in function notation for the situation.

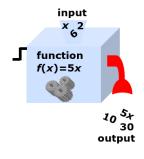
An amusement park charges a \$6.00 parking fee plus \$29.99 per person.

Helpful Hint

There are several different ways to describe the variables of a function.

Independent Variable	Dependent Variable
x-values	y-values
Domain	Range
Input	Output
X	<i>f</i> (<i>x</i>)

You can think of a function as an input-output machine.



Evaluating Functions

<u>Example 1</u> – All Done for You! Evaluate the function for the given input values.

For $f(x) = 3x + 2$, find $f(x)$ when $x = 7$ and when $x = -4$.				
	$f(\mathbf{x}) = 3(x) + 2$		f(x) = 3(x) + 2	
	f(7) = 3(7) + 2	Substitute 7 for x.	f(-4) = 3(-4) + 2	Substitute –4 for x.
	= <mark>21</mark> + 2	Simplify.	= -12 + 2	Simplify.
	= 23		= -10	

<u>Example 2</u> – Let's Try This One Together! Evaluate the function for the given input values.

Given: g(t) = 1.5t - 5 Find: g(t) when t = 6 and when t = -2

Example 3 - You Try!

(a) Given:
$$g(t) = \frac{1}{4}t + 1$$
 Find: $g(t)$ when $t = -24$ and when $t = 400$

(b) Given:
$$h(r) = \frac{1}{3}r + 2$$
 Find: $h(r)$ when $r = 600$ and when $r = -12$

When a function describes a real-world situation, every real number is not always reasonable for the domain and range. For example, a number representing the length of an object Cannot be negative, and only whole numbers can represent a number of people.

Finding the Reasonable Range and Domain of a Function

<u>Example 1</u>

Write a function to describe the situation. Find a reasonable domain and range of the function. Joe has enough money to buy 1, 2, or 3 DVDs at \$15.00 each.

Money spent f(x)	is =	\$15.00 \$15.00	for each •	DVD. <i>x</i>	
If Joe buys x DVDs, he will spend $f(x) =$					
So, Joe only has enough money to purchase					

}

}

}

Substitute the domain values into the function rule to find the range values.

X	1	2	3
f (x)			

So a reasonable range would be: $\{$

<u>Example 2</u>

Write a function to describe the situation. Find a reasonable domain and range of the function.

The settings on a space heater are the whole numbers from 0 to 3. The total of watts used for each setting is 500 times the setting number. Write a function rule to describe the number of watts used for each setting. Find a reasonable domain and range for the function.

Number of is 500 times the setting #. watts used f(x) =

For each setting, the number of watts is f(x) =

There are 4 possible settings ______ so a reasonable domain would be: {

x	0	1	2	3
f(x)				

So, a reasonable range for this situation is $\{$

LESSON Practice B	
4-3 Writing Functions	
Determine a relationship between the <i>x</i> - ar equation.	nd y-values. Write an
1. x -4 -3 -2 -1 y -1 0 1 2	2. {(2, 3), (3, 5), (4, 7), (5, 9)}
Identify the independent and dependent va	ariables in each situation.
 Ice cream sales increase when the temperature rises. I: 	 4. Food for the catered party costs \$12.75 per person. I:
D:	D:
Identify the independent and dependent va function notation for each situation. 5. Carson charges \$7 per hour for yard work.	
Evaluate each function for the given input	values.
7. For $f(x) = 5x + 1$, find $f(x)$ when $x = 2$ and y	when <i>x</i> = 3
8. For $g(x) = -4x$, find $g(x)$ when $x = -6$ and y	when x = 2
9. For $h(x) = x - 3$, find $h(x)$ when $x = 3$ and y	when x = 1
Complete the following.	
10. An aerobics class is being offered once a week for 6 weeks. The registration fee is and the cost for each class attended is \$1 Write a function rule to describe the total the class. Find a reasonable domain and for the function.	\$15 10. cost of

LESSON Practice C

4-3

Writing Functions

Determine a relationship between the *x*- and *y*-values. Write an equation.

1.					
	x	-2	-1	0	1
	у	4	1	0	1

2. $\{(-1, -4), (0, -2), (2, 2), (5, 8)\}$

Identify the independent and dependent variables in each situation.

- More program money is given out to cities with a larger population.
 - l: _____
 - D: _____
- Sales tax in the state of Maryland is 5% of the purchase price.

l:

D: _____

Identify the independent and dependent variables. Write a rule in function notation for each situation.

- Meg earns a \$5 flat fee plus \$4.50 per student for a tutoring session.
- Jeb is allowed 2 hours less television time per week than his older brother.

Evaluate each function for the given input values.

- 7. For f(x) = 3x + 2, find f(x) when x = 4 and when x = -1.
- For g(x) = -6x, find g(x) when x = -5 and when x = 3.
- 9. For *h*(*x*) = *x*² 4, find *h*(*x*) when *x* = 2 and when *x* = -7. _____

Complete the following.

10. A fitness class is being offered twice a week for four weeks. The registration fee is \$8.50 and the cost for each class attended is \$4.75. Write a function rule to describe the total cost of the class. Find a reasonable domain and range for the function.

LESSON Review for Mastery

4-3 Writing Functions

Functions have dependent and independent variables. The dependent variable will always depend on the independent variable.

Rewrite each situation using the word *depends*. Then identify the dependent and the independent variables.

An employee who works longer hours will receive a larger amount in her paycheck.

Rewrite sentence:

The amount of a paycheck depends on the number of hours worked.

Dependent: amount of paycheck Independent: number of hours worked

A box with several books weighs more than a box with just a few books.

Rewrite sentence:

The weight of a box depends on the number of books in the box.

Dependent: weight of box Independent: number of books in box

Rewrite each sentence using the word *depends*. Then identify the dependent and the independent variables.

1. A very large animal will eat many pounds of food.

Dependent:

Independent:

2. The fire was very large, so many firefighters were there.

Dependent:

Independent: _____

3. The temperature of the water on the heated stove rose each minute.

Dependent:

Independent: _____

4. The restaurant bill was low because only a few meals were ordered.

Dependent: _____

LESSON Review for Mastery 4-3 Writing Functions continued After identifying the independent and dependent variables, you can write a rule in function notation. Remember that f(x) is the dependent variable and x is the independent variable. Identify the dependent and independent variables. Write a function rule for each situation. A zoo charges \$6 for parking and \$17.50 for each child. 1. Identify the dependent and independent variables. The cost of admission depends on the number of children. Dependent f(x): cost of admission Independent x: number of children 2. Write the equation in words. The cost of admission is \$17.50 multiplied by the number of children plus \$6 for parking. Write the function using cost of admission = f(x) and number of children = x. f(x) = \$17.50x + \$6.00Evaluate the function above when x = 4 and x = 10. x = 4x = 10f(x) = \$17.50x + \$6.00f(x) = \$17.50x + \$6.00f(4) = \$17.50(4) + \$6.00f(10) =\$17.50(10) + \$6.00 = \$70.00 + \$6.00 = \$175.00 + \$6.00 = \$76.00 = \$181.00

Identify the dependent and the independent variables for each situation below. Write the function. Then evaluate the function for the given input values.

5. A	A limo	service	charges	\$90 for	each hour	-
------	--------	---------	---------	----------	-----------	---

Dependent f(x):	
Independent x:	
Function:	
Evaluate for $x = 2$	2.

6.	A computer support company charges
	\$295 for the first hour plus \$95 for each
	additional hour.

Dependent f(x)	:
----------------	---

Independent x:	

Function:

Evaluate for x = 3.25.

Evaluate for x = 7.5.

Evaluate for x = 8.

LESSON Problem Solving

Writing Functions

Identify the independent and dependent variables. Write a rule in function notation for each situation.

 Each state receives electoral votes based on the number of representatives it has in the House of Representatives.

Representatives	2	4	6	8
Electoral Votes	4	6	8	10

Terry has 30 pieces of gum and gives 2 pieces to each of his friends.

- Ronaldo is buying bacon that costs \$4.29 per pound.
- A personal trainer charges \$50 for the first session and \$40 for every session thereafter.

International travel and business require the conversion of American dollars into foreign currency. During part of 2005, one American dollar was worth 6 Croatian Kuna. Select the best answer.

5. An American bank wishes to convert d dollars into kuna. Which function rule describes the situation?

A
$$f(d) = \frac{d}{6}$$
 C $f(d) = \frac{6}{d}$

$$B f(d) = 6d$$
 $D f(d) = d + 6$

 Macon has \$100 and is thinking about converting some of it into kuna. What is a reasonable range for this situation?

A $0 \le y \le 6$ C $0 \le y \le 100$

B
$$0 \le y \le 16.7$$
 D $0 \le y \le 600$

8. Robin converts x dollars into y kuna. Which expression is the independent variable in this situation?

Fx	H 6x
Gy	J 6y

6. A Croatian company already has \$100,000 and is going to convert k kuna into dollars. Which function rule can be used to determine the total amount of American dollars this company will have?

F
$$f(x) = 100,000 + 6k$$

G $f(x) = 100,000 + \frac{k}{6}$
H $f(x) = 100,000k + 6$
J $f(x) = 100,000 + \frac{6}{k}$

9. Jakov converts n kuna into c dollars. Which expression is the dependent variable in this situation?

A n	С <u>п</u>
Вc	$D \frac{c}{6}$



~ Section 4.4 Notes ~ Graphing Functions

TLW graph functions given a limited domain

TLW graph functions given a domain of all real numbers

TLW graph functions using concepts learned in section 4.3 of evaluating functions at a given value



<u>Quick Draw Review</u> In 1 - 3, solve each equation for y.

1. 2x + y = 3

2. -x + 3y = -6

3. 4x - 2y = 8

4. Generate ordered pairs for
$$y = \frac{1}{2}x + 1$$
 using $x = -4, -2, 0, 2$, and 4

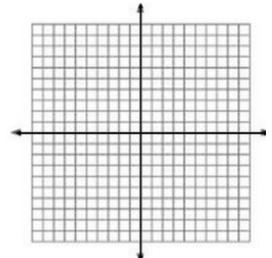
Scientists can use a function to make conclusions about the rising sea level.

Sea level is rising at an approximate rate of 2.5 millimeters per year. If this rate continues, the function y = 2.5x Can describe how many millimeters y sea level will rise in the next x years.

32

You Can graph a function by finding ordered pairs that satisfy the function.

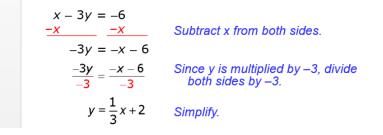
х	у



Example 1 - All Done for You!

Graph the function for the given domain. x - 3y = -6; D: $\{-3, 0, 3, 6\}$

Step 1 Solve for y since you are given values of the domain, or x.



Step 2 Substitute the given value of the domain for *x* and find values of *y*.

x	$y=\frac{1}{3}x+2$	(x, y)
-3	$\frac{1}{3}(-3) + 2 = 1$	(-3, 1)
0	$\frac{1}{3}(0) + 2 = 2$	(0, 2)
3	$\frac{1}{3}(3) + 2 = 2$	(3, 3)
6	$\frac{1}{3}(6) + 2 = 4$	(6, 4)

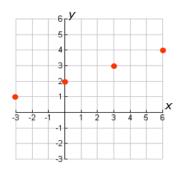
Example 2 – Let's Try This One Together! Graph the function for the given domain.

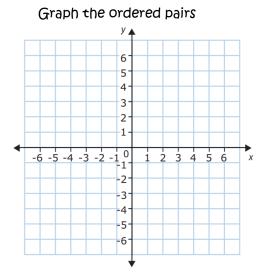
 $f(x) = x^2 - 3; D: \{-2, -1, 0, 1, 2\}$

Use the given values of the domain to find the values of f(x)

x	$f(x) = x^2 - 3$	(x, f(x))
-2		
-1		
0		
1		
2		

Step 3 Graph the ordered pairs.

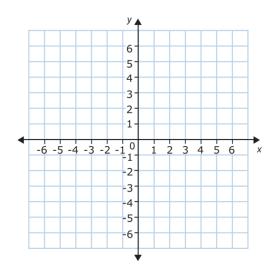




Example 3 – You Try! Graph the function for the given domain.

 $-2x + y = 3 \qquad D: \{-5, -3, 1, 4\}$

x	y=2x+3	(<i>x</i> , <i>y</i>)
-5		
-3		
1		
4		



If the domain of a function is all real numbers, any number can be used as an input value. This process will produce an infinite number of ordered pairs that satisfy the function. Therefore, arrowheads are drawn at both "ends" of a smooth line or curve to represent the infinite number of ordered pairs. If a domain is not given, assume that the domain is all real numbers.

Graphing Functions Using a Domain of All Real Numbers		
Step 1	Use the function to generate ordered pairs by choosing several values for x .	
Step 2	Plot enough points to see a pattern for the graph.	
Step 3	Connect the points with a line or smooth curve.	

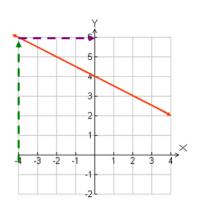
Finding Values Using Graphs

Example 1 - All Done for You!

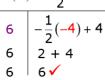
Use a graph of the function $f(x) = -\frac{1}{2}x + 4$ to find the value of f(x) when x = -4.

Check your answer algebraically.

Locate -4 on the *x*-axis. Move up to the graph of the function. Then move right to the *y*-axis to find the corresponding value of *y*. f(-4) = 6

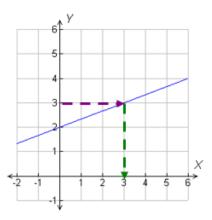


f(-4) = 6**Check** Use substitution. $f(x) = -\frac{1}{2}x + 4$



Example 2 – Let's Try This One Together

Use a graph of the function $f(x) = \frac{1}{3}x + 2$ to find the value of f(x) when x = 3. Check your answer algebraically.



Recall that in real-world situations you may have to limit the domain to make answers reasonable. For example, quantities such as time, distance, and number of people Can be represented using only nonnegative values. When both the domain and the range are limited to nonnegative values, the function is graphed only in Quadrant I.

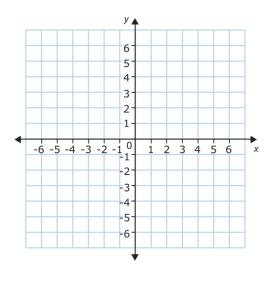
Problem Solving Applications

Example 1 – Let's Try This Together

A mouse can run 3.5 meters per second. The function y = 3.5x describes the distance in meters the mouse can run in x seconds. Graph the function. Use the graph to estimate how many meters a mouse can run in 2.5 seconds.

Choose several nonnegative values of x to find values of y.

x	y = 3.5x	(x, y)
0		
1		
2		
3		

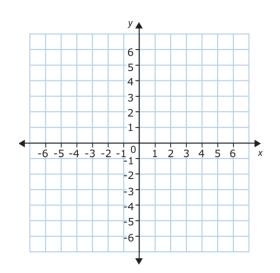


So to answer the question, a mouse Can run about _____ meters in 2.5 seconds.

Guided Practice

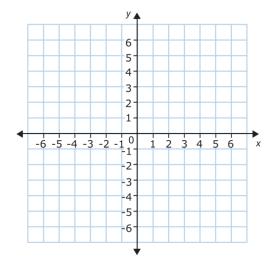
1. Graph the function: -3x + 2 = y

x	-3x+2=y	(<i>x,</i> y)
-2		
-1		
0		
1		
2		
3		



2. Graph the function: y = |x-1|

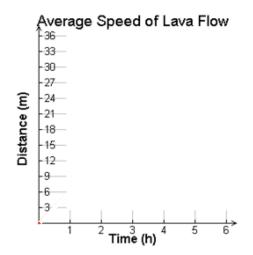
x	(<i>x, y</i>)
-2	
-1	
0	
1	
2	
3	

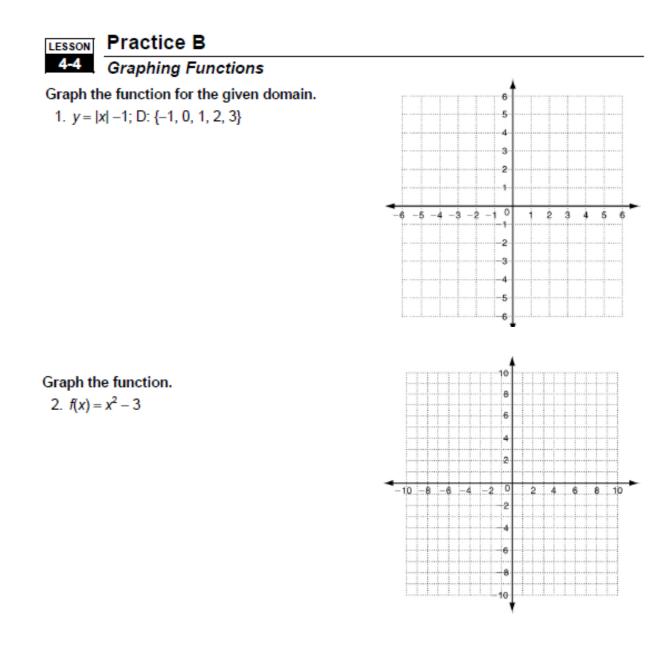


3. The fastest recorded Hawaiian lava flow moved at an average speed of 6 miles per hour. The function y = 6x describes the distance y the lava moved on average in x hours. Graph the function. Use the graph to estimate how many miles the lava moved after 5.5 hours.

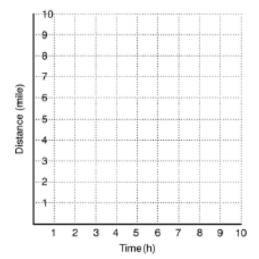
x	<i>y</i> = б <i>x</i>	(<i>x, y</i>)
1		
3		
5		

The lava will travel about _____ meters in 5.5 seconds.





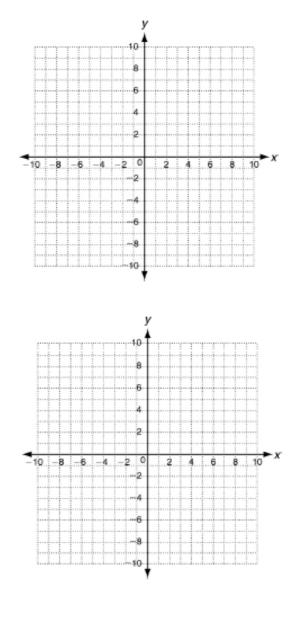
3. One of the slowest fish is the blenny fish. The function y = 0.5x describes how many miles y the fish swims in x hours. Graph the function. Use the graph to estimate the number of miles the fish swims in 3.5 hours.



LESSON Practice C

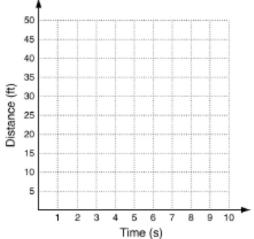
4-4 Graphing Functions

1. Graph y = |x - 2| + 3 for the following domain: {-2, 0, 2, 4, 6}



2. Graph $y = \left(\frac{x}{4}\right)^2 + 2$.

3. A human being can swim at a maximum rate of 7.4 feet per second. The function y = 7.4x describes how many feet y a person can swim in x seconds. Graph the function. Use the graph to estimate the maximum number of feet a person can swim in 4.5 seconds.





LESSON Problem Solving

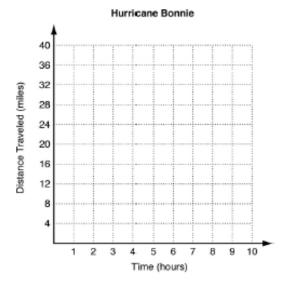
Graphing Functions

In 1998, Hurricane Bonnie approached the United States at a speed of 8 miles per hour. The function y = 8x describes how many miles y Hurricane Bonnie traveled in x hours.

1. Complete the table by generating ordered pairs.

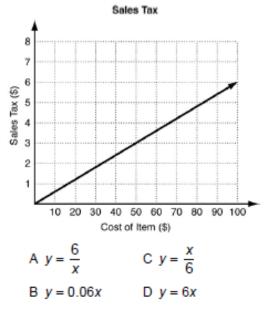
x	y = 8x	(x, y)
0		
1		
2		
3		
4		

3. Use the graph to estimate how far Hurricane Bonnie traveled in 3.5 hours. Graph the function y = 8x.

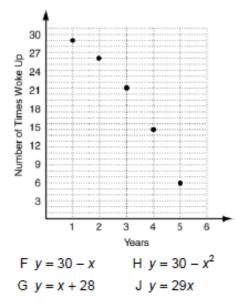


Select the correct answer.

4. The graph below shows the relation between the cost of an item and the sales tax due. Which function is graphed below?



The graph below shows the relation between Jeremy's age and the number of times per year he refused to eat his brussel sprouts. Which function is graphed for the domain {1, 2, 3, 4, 5}?



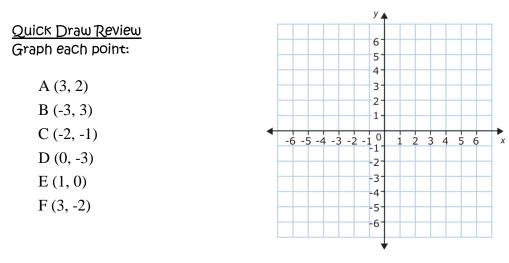
~ Section 4.5 Notes ~ Scatter Plots and Trend Lines

TLW create and interpret scatter plots

TLW use trend lines to make predictions

TLW define new vocabulary words: scatter plot, correlation, positive correlation, negative correlation, no correlation, and trend line



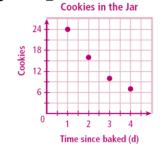


Graphing a Scatter Plot from Given Data

Example 1 - All Done for You!

The table shows the number of cookies in a jar from the time since they were baked. Graph a scatter plot using the given data.

Cookies in the Jar						
Time Since Baked (d)	1	2	3	4		
Cookies	24	16	10	7		



Use the table to make ordered pairs for the scatter plot.

The x-value represents the time since the cookies were baked and the y-value represents the number of cookies left in the jar.

Plot the ordered pairs.

Displaying data visually Can help you see relationships.

A

is a graph with points plotted to show a possible relationship between two sets of data.

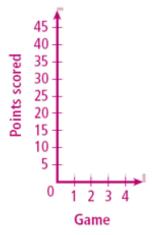
A scatter plot is an effective way to some types of data.

Example 2 - Let's Try this one Together!

The table shows the number of points scored by a high school football team in the first four games of a season. Graph a scatter plot using the given data.

Game	1	2	3	4
Score	6	21	46	34

Football Team Scores

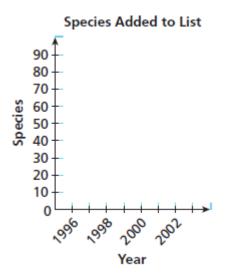


Example 3 - You Try!

The table shows the number of species added to the list of endangered and threatened species in the United States during the given years. Graph a scatter plot using the given data.

Increase in List							
Calendar Year	1996	1997	1998	1999	2000	2001	2002
Species	91	79	62	11	39	10	9

Source: U.S. Fish and Wildlife Service



A

describes a relationship between two data sets.

A graph may show the Correlation between data. The Correlation Can help you analyze trends and make predictions.

There are three types of correlations between data.

Correlations

Positive Correlation

Both sets of data values increase.



Negative Correlation

One set of data values increases as the other set decreases.



No Correlation

There is no relationship between the data sets.

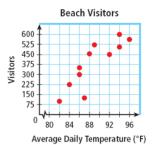


Example 1 - All Done for You!

Describe the correlation illustrated by the scatter plot.

As the average daily temperature increased, the number of visitor increased.

There is a positive correlation between the two data sets.





Example 2 - Let's Try this One Together!

Describe the correlation illustrated by the scatter plot.

As the years passed in the snowboarding competition _____ .

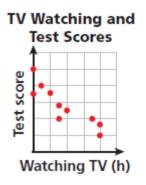
There is a	Correlation between
the two sets of data.	

Example 3 – You Try! Describe the correlation illustrated by the scatter plot.

As_____

There is a _____ Correlation between the two sets of data.





Identifying Correlations

Example 1 – All Done for You!

Identify the correlation you would expect to see between the pair of data sets. Explain.

the number of people in an audience and ticket sales

You would expect to see a positive correlation. As the number of people in the audience increases, ticket sales increase.

Example 2 - Let's Try this One Together

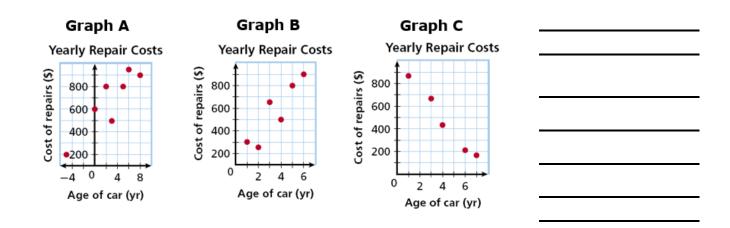
Identify the correlation you would expect to see between the pair of data sets. Explain.

the number of people in an audience and	d ticket sales
You would expect to see a	
As the number of people in the audience	, tiCket sales
Examples 3 & 4 – You Try! Identify the Correlation you would expect to so a runner's time and the distance to the f	inish line
You would expect to see a	
As a runner's time	, the distance to the finish line
the temperature in Houston and the num	nber of cars sold in Boston
You would expect to see a	·
The temperature in Houston	the number of Cars sold in Boston.

Matching Scatter Plots to Situations

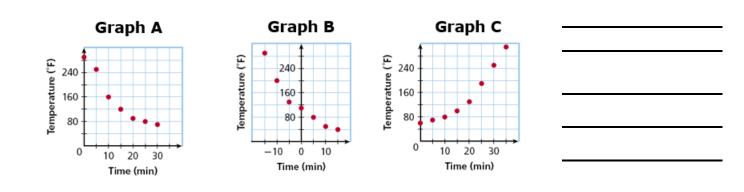
Choose the scatter plot that best represents

the relationship between the age of a car and the amount of money spent each year on repairs Explain.



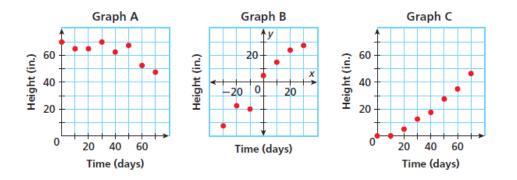
Choose the scatter plot that best represents

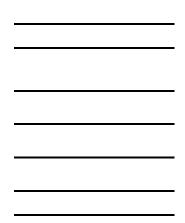
the relationship between the number of minutes since a pie has been taken out of the oven and the temperature of the pie Explain.



Choose the scatter plot that best represents

the relationship between the number of days since a sunflower seed was planted and the height of the plant Explain.





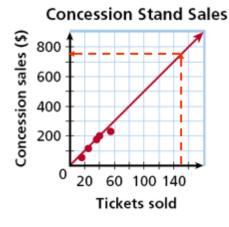
You Can graph a function on a scatter plot to help show a relationship in the data. Sometimes the function is a straight line. This line, Called a ______, helps show the correlation between data sets more Clearly. It Can also be helpful when making predictions based on the data.

Application Examples- Trend Lines

Example 1 – Let's Try this One Together

The scatter plot shows a relationship between the total amount of money collected at the concession stand and the total number of tickets sold at a movie theater. Based on this relationship, predict how much money will be collected at the concession stand when 150 tickets have been sold.

Draw a trend line and use it to make a prediction.

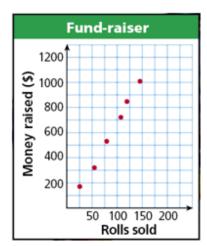


Based on the data, ______ is a reasonable prediction of how much money will be collected when 150 tickets have been sold.

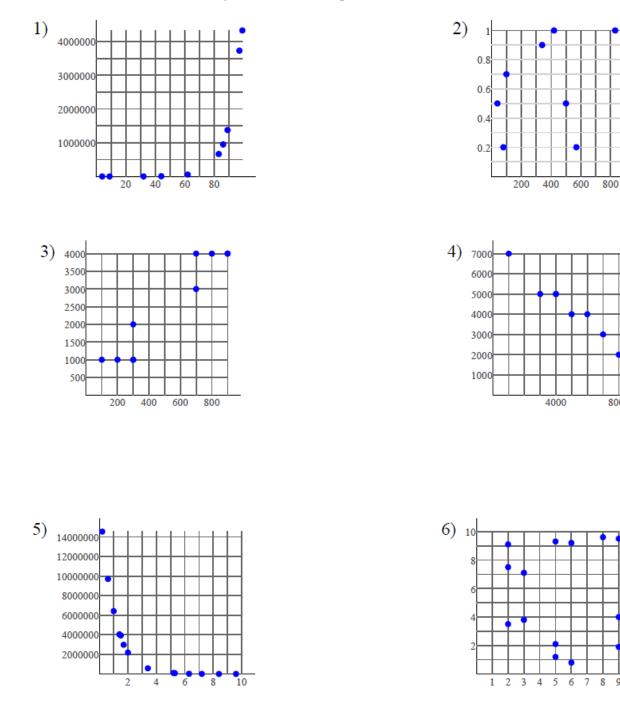
Example 2 - You Try!

Based on the trend line, predict how many wrapping paper rolls need to be sold to raise \$500.

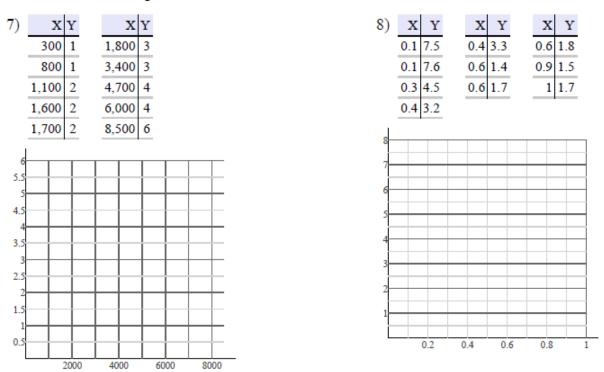
Based on the data, about ______ wrapping paper rolls is a reasonable prediction of how many rolls need to be sold to raise \$500.



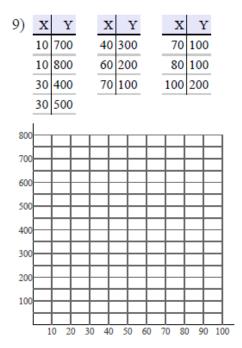
State if there appears to be a positive correlation, negative correlation, or no correlation. When there is a correlation, identify the relationship as linear or nonlinear.

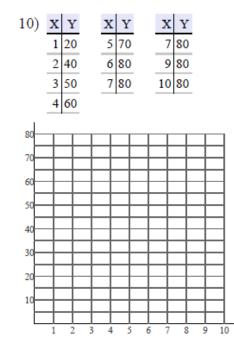


Construct a scatter plot.



Construct a scatter plot. Find the slope-intercept form of the equation of the line that best fits the data.





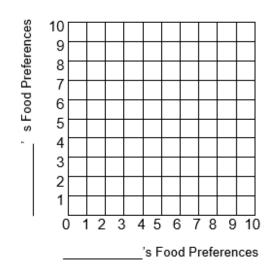
This activity is designed to help you to learn about scatterplots and correlation. In order to complete the activity you will need a partner.

- 1. Before finding a partner, rank the following ten cafeteria foods in order from the food you like the most to the food you like the least.
 - 1. Pizza
 - 2. Steak
 - 3. Hamburger
 - 4. Fries
 - 5. Pretzel
 - 6. Salad
 - 7. Cookies
 - 8. Chicken Sandwiches
 - 9. Ice Cream
 - 10. Popsicles

Record your preferences below:

The number of the food I like the most is:
The number of the food I like 2 nd most is:
The number of the food I like 3 rd most is:
The number of the food I like 4 th most is:
The number of the food I like 5 th most is:
The number of the food I like 6 th most is:
The number of the food I like 7 th most is:
The number of the food I like 8 th most is:
The number of the food I like 9 th most is:
The number of the food I like the least:

- 2. Now get together with your partner. Write your responses for the 10 items above as ordered pairs. For example, if your 1st favorite food is pizza and your partner's favorite food is Fries, write the ordered pair (1, 4). Then go on to the food you both like second most. You will have 10 ordered pairs. Whoever uses their choice as the x-coordinate should remain the x-coordinate for all 10 ordered pairs. List the ordered pairs here: ______
- 3. Plot your 10 points on the coordinate plane below.



4. Analyze the Data:

- The stronger the positive association, the more likely you and your partner would enjoy going out to eat together.
- The stronger the negative association, the less likely you and your partner would enjoy going out to eat together.
- If the association is weak, then your agreement on dinner would be hit and miss.

What conclusions can you draw based upon your scatterplot?

LESSON Practice B

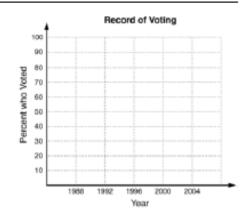
4-5

Scatter Plots and Trend Lines

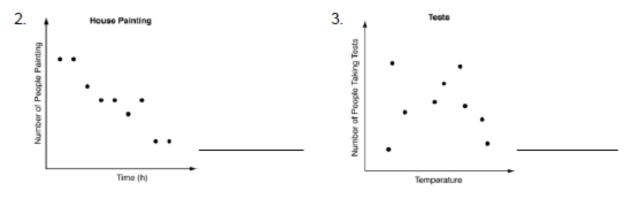
Graph a scatter plot using the given data.

 The table shows the percent of people ages 18–24 who reported they voted in the presidential elections. Graph a scatter plot using the given data.

Year	1988	1992	1996	2000	2004
% of 18-24 year olds	56	43	32	32	42



Write *positive*, *negative*, or *none* to describe the correlation illustrated by each scatter plot.

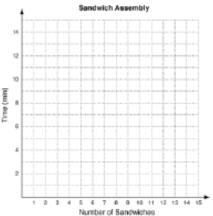


Identify the correlation you would expect to see between the number of pets a person has and the number of times they go to a pet store. Explain.

Neal kept track of the number of minutes it took him to assemble sandwiches at his restaurant. The information is in the table below.

Number of sandwiches	1	2	4	6	7
Minutes	3	4	5	6	7

- 5. Graph a scatter plot of the data.
- 6. Draw a trend line.
- 7. Describe the correlation.
- Based on the trend line you drew, predict the amount of time it will take Neal to assemble 12 sandwiches.



LESSON Practice C

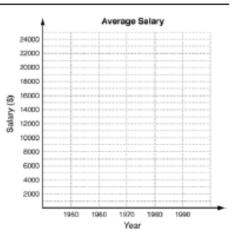
4-5

Scatter Plots and Trend Lines

Graph a scatter plot using the given data.

 The table shows the average salary (rounded to the nearest hundred) for one type of worker, listed by decade. Graph a scatter plot using the given data.

Decade	1950	1960	1970	1980	1990
Avg. Salary	\$2800	\$4800	\$8300	\$15,400	\$23,700



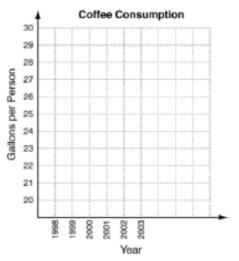
Identify the correlation you would expect to see between the pair of data sets. Explain.

- 2. The number of chicken pox vaccines given and the number of chicken pox cases reported.
- 3. The number of vacation days given to employees and their level of job satisfaction.

The average number of gallons of coffee per person consumed in the United States is shown in the table below.

Years	1998	1999	2000	2001	2002	2003
Avg. annual per capita consumption	23.9	25.1	26.3	24.2	23.6	24.3

- 4. Graph a scatter plot of the data.
- 5. Draw a trend line.
- 6. Describe the correlation.
- Based on the trend line you drew, predict the average amount of coffee consumed per person in 2007.
- 8. How confident are you in your prediction? Explain.



Problem Solving

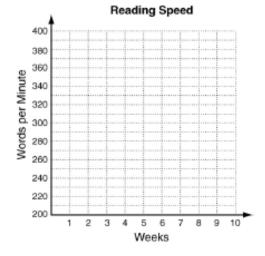
LESSON 4-5

Scatter Plots and Trend Lines

Fawn is trying to improve her reading skills by taking a speedreading class. She is measuring how many words per minute (wpm) she can read after each week of the class.

 Graph a scatter plot using the given data.

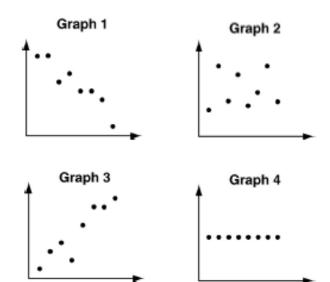
Weeks	1	2	3	4	5
wpm	220	230	260	260	280



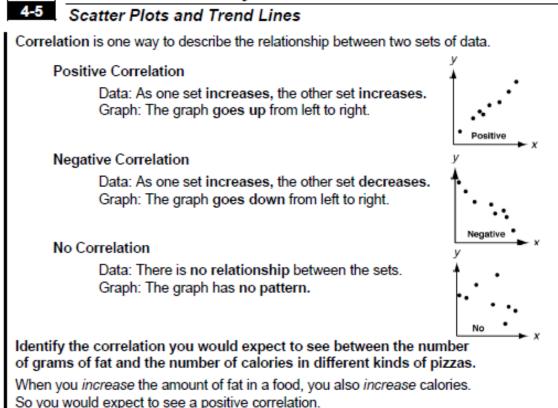
- Describe the correlation illustrated by the scatter plot.
- Draw a trend line and use it to predict the number of words per minute that Fawn will read after 8 weeks of this class.
- Fawn is paying for this class each week out of her savings account. Identify the correlation between the number of classes and Fawn's account balance.

Choose the scatter plot that best represents the described relationship.

- the distance a person runs and how physically tired that person is
 - A Graph 1 C Graph 3
 - B Graph 2 D Graph 4
- the price of a new car and the number of hours in a day
 - F Graph 1 H Graph 3
 - G Graph 2 J Graph 4
- a person's age and the amount of broccoli the person eats
 - A Graph 1 C Graph 3
 - B Graph 2 D Graph 4
- the number of cats in a barn and the number of mice in that barn
 - F Graph 1 H Graph 3
 - G Graph 2 J Graph 4



LESSON Review for Mastery

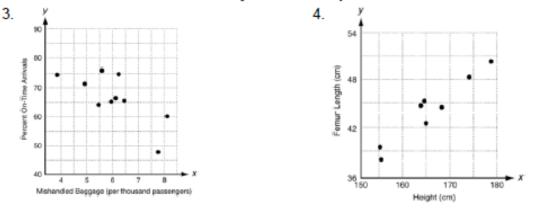


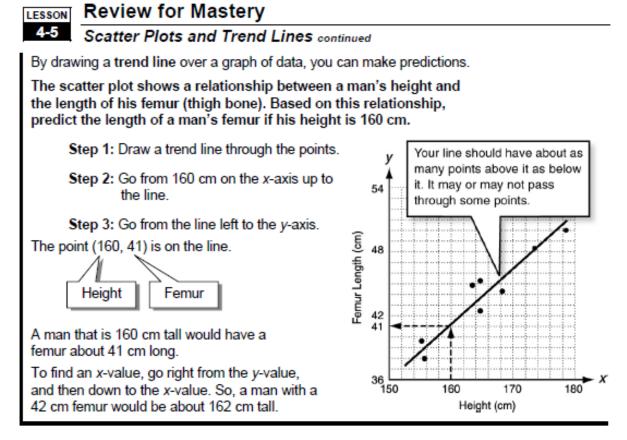
Identify the correlation you would expect to see between

each pair of data sets. Explain.

- 1. the number of knots tied in a rope and the length of the rope
- 2. the height of a woman and her score on an algebra test

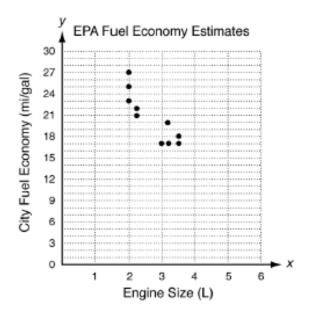
Describe the correlation illustrated by each scatter plot.





The scatter plot shows a relationship between engine size and city fuel economy for ten automobiles.

- 5. Draw a trend line on the graph.
- 6. Based on the relationship, predict...
 - a. the city fuel economy of an automobile with an engine size of 5 L.
 - b. the city fuel economy of an automobile with an engine size of 2.8 L.
 - c. the engine size of an automobile with a city fuel economy of 11 mi/gal.
 - d. the engine size of an automobile with a city fuel economy of 28 mi/gal.

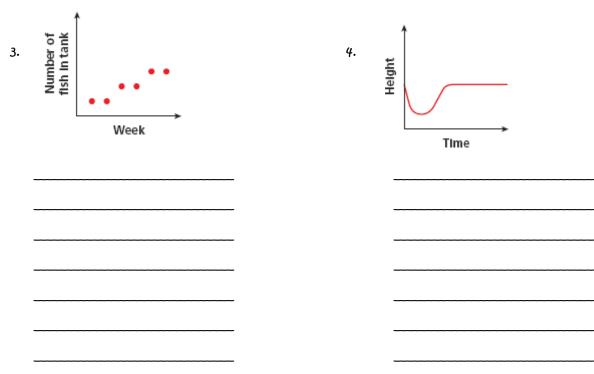


Sketch a graph for each situation. Label the x and y axis. Tell whether the graph is continuous or discrete.

1. A girl was walking home at a steady pace. Then she stopped to talk to a friend. After her friend left, she jogged the rest of the way home.

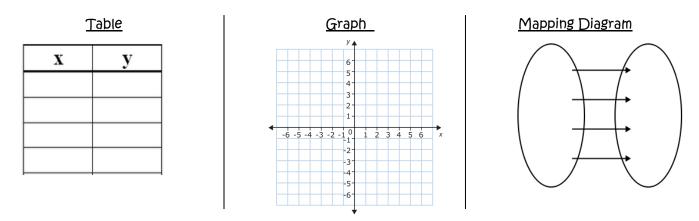
2. A ball is dropped from a second story window and bounces to a stop on the patio below.

Write a possible situation for each graph.

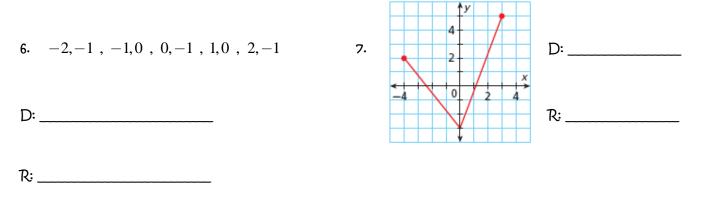


Express the relation as a table, graph, and mapping diagram.

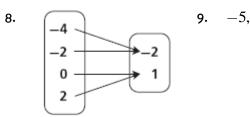
5. -1,0 , 0,1 , 2,1 , -3,4



Give the domain and range of each relation.



Determine if the relation is a function or not. Write yes or no on the line.



9. -5, -3, -3, -2, -1, -1, 1, 0 10

	x	1	2	3
0.	у	3	2	1

4

0

1

-1

Determine the relationship between x and y. Write an equation on the line.

x					
у	-6	-5	-4	-3	

Identify the dependent and independent variables. Write and equation in function notation for the situation.

13. A baker spends \$6 on ingredients for each Cake he bakes.

Dependent:	Independen t :
Function:	
Arlando will buy twice as many CDs	s as Dante.
Dependen t :	Independen t :

Function:

14.

15. For f(x) = -2x + 4, find f(x) when x = -5

16. For $g(x) = -x^2 - 2$, find g(x) when x = -3

Graph each function for the given domain.

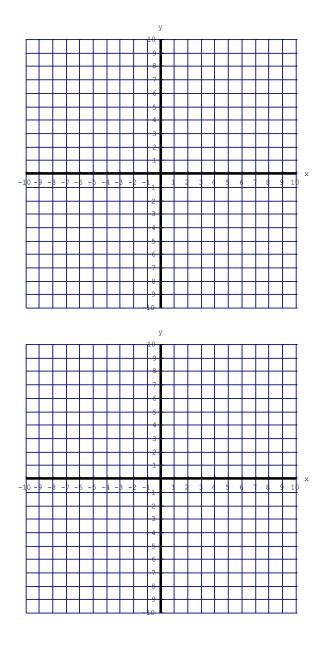
17. 4x + y = 2 D: -2, -1, 1, 2

×	y =	(X,Y)

Graph each function.

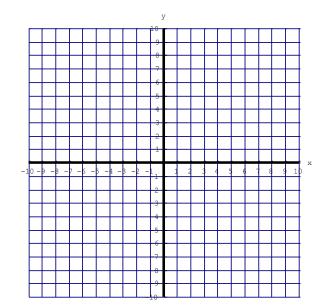
18. $y = x^2 - 6$

×	у =	(X,Y)



19.
$$y = 2 - |x|$$

×	y =	(X,Y)



20. 3x - y = 1

×	y =	(X,Y)

